

# ETAP Unbalanced Load Flow

The ETAP V&V process for the Unbalanced Load Flow program has over 550 test case scenarios that are run before each ETAP release. The following cases are excerpts from the Unbalanced Load Flow V&V documentation.

## Unbalanced Load Flow Comparison Case # 1

### Comparison of ETAP Unbalanced Load Flow Results against a Published IEEE 13-Bus Feeder System

#### Excerpts from Validation Cases and Comparison Results (TCS-ULF-002)

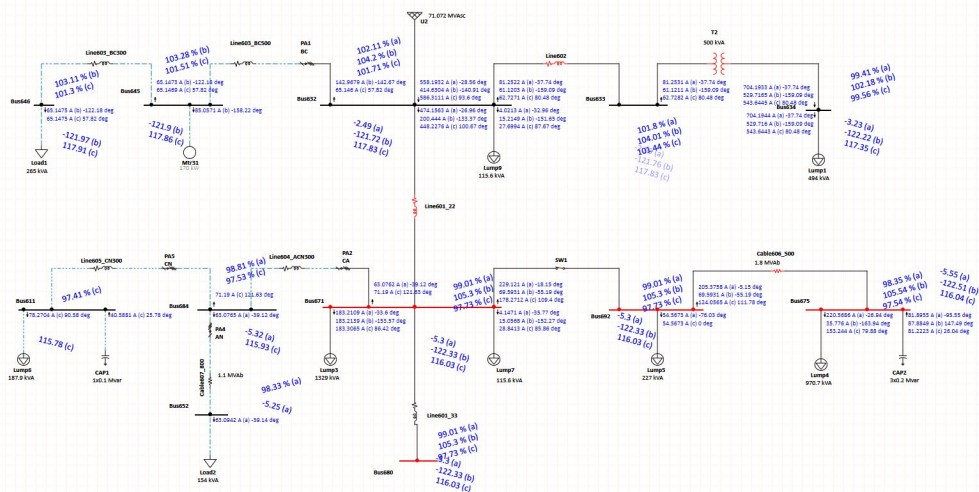
##### Highlights

- Comparison of ETAP Unbalanced Load Flow (ULF) results against those published in Radial Test Feeders - IEEE Distribution System Analysis Subcommittee for an IEEE 13-bus feeder system found on <https://cmte.ieee.org/pes-testfeeders/resources/>.
- Comparison of bus voltages and angles on each phase.
- Comparison of current flows and angles on each phase.
- The difference in the results is less than 0.5% for all bus voltages and power flows.

##### System Description

To model the unbalanced distribution thirteen-bus system found in the web site above, an equivalent system (as shown in Figure 1) was designed in ETAP with the following conditions:

1. This case covers only the portion below Node 632 due to the same ETAP transformer tap for three phases.
2. The portion above Node 632 is modeled using the internal impedances of the utility.
3. Cables are modeled using impedances.
4. The distributed load is modeled using two lumped loads at both line terminals.
5. The single-phase load of constant current is modeled using an approximate lumped load.



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### Comparison of Results

The following tables of comparison show the differences between ETAP results and those published on the IEEE 13-bus feeder. Please note that the percent difference for all branch flows and bus voltages is less than 0.5%. Any missing fields in the tables below were not provided in the IEEE benchmark results; however, the corresponding ETAP results have been included.

Bus	Voltage in %								
	Phase A			Phase B			Phase C		
	IEEE	ETAP	% Diff	IEEE	ETAP	% Diff	IEEE	ETAP	% Diff
632	102.10	102.11	<b>0.01</b>	104.20	104.20	<b>0.00</b>	101.74	101.71	<b>-0.03</b>
633	101.80	101.80	<b>0.00</b>	104.01	104.01	<b>0.00</b>	101.48	101.44	<b>-0.04</b>
634(XF13)	99.40	99.41	<b>0.01</b>	102.18	102.18	<b>0.00</b>	99.60	99.56	<b>-0.04</b>
645	-	-	-	103.29	103.28	<b>-0.01</b>	101.55	101.51	<b>-0.04</b>
646	-	-	-	103.11	103.11	<b>0.00</b>	101.34	101.30	<b>-0.04</b>
671	99.00	99.01	<b>0.01</b>	105.29	105.30	<b>0.01</b>	97.78	97.73	<b>-0.05</b>
680	99.00	99.01	<b>0.01</b>	105.29	105.30	<b>0.01</b>	97.78	97.73	<b>-0.05</b>
684	98.81	98.81	<b>0.00</b>	-	-	-	97.58	97.53	<b>-0.05</b>
611	-	-	-	-	-	-	97.38	97.41	<b>0.03</b>
652	98.25	98.33	<b>0.08</b>	-	-	-	-	-	-
692	99.00	99.01	<b>0.01</b>	105.29	105.30	<b>0.01</b>	97.77	97.73	<b>-0.04</b>
675	98.35	98.35	<b>0.00</b>	104.20	104.20	<b>0.00</b>	97.58	97.54	<b>-0.04</b>

Table 1: Bus Voltage Magnitude Comparison

Bus	Phase angle in Degrees								
	Phase A			Phase B			Phase C		
	IEEE	ETAP	% Diff	IEEE	ETAP	% Diff	IEEE	ETAP	% Diff
632	-2.49	-2.49	<b>0.00</b>	-121.72	-121.72	<b>0.00</b>	117.83	117.83	<b>0.00</b>
633	-2.56	-2.55	<b>-0.39</b>	-121.77	-121.76	<b>-0.01</b>	117.82	117.83	<b>-0.01</b>
634(XF13)	-3.23	-3.23	<b>0.00</b>	-122.22	-122.22	<b>0.00</b>	117.34	117.35	<b>-0.01</b>
645	-	-	-	-121.9	-121.90	<b>0.00</b>	117.86	117.86	<b>0.00</b>
646	-	-	-	-121.98	-121.97	<b>-0.01</b>	117.9	117.91	<b>-0.01</b>
671	-5.30	-5.30	<b>0.00</b>	-122.34	-122.33	<b>-0.01</b>	116.02	116.03	<b>-0.01</b>
680	-5.30	-5.30	<b>0.00</b>	-122.34	-122.33	<b>-0.01</b>	116.02	116.03	<b>-0.01</b>
684	-5.32	-5.32	<b>0.00</b>	-	-	-	115.92	115.93	<b>-0.01</b>
611	-	-	-	-	-	-	115.78	115.78	<b>0.00</b>
652	-5.25	-5.25	<b>0.00</b>	-	-	-	-	-	-
692	-5.31	-5.30	<b>-0.19</b>	-122.34	-122.33	<b>-0.01</b>	116.02	116.03	<b>-0.01</b>
675	-5.56	-5.55	<b>-0.18</b>	-122.52	-122.51	<b>-0.01</b>	116.03	116.04	<b>-0.01</b>

Table 2: Bus Voltage Angle Comparison

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To model the distributed load along node “Bus632” to node “Bus671”, the loading is equally connected at each end of the line segment (Line601\_22), i.e. Lump9 and Lump7. Therefore, the current flows going from Bus632 to Bus671 and vice-versa are the following:

$$\begin{aligned}
 &^1 632-671: \quad \text{Phase A: } 474.16\angle-26.94+ 4.02\angle-32.96 = 478.16\angle-27.01 \\
 & \quad \quad \quad \text{Phase B: } 200.44\angle-133.37+15.2\angle-151.65 = 214.93\angle-134.64 \\
 & \quad \quad \quad \text{Phase C: } 448.23\angle100.67+ 27.7\angle87.67= 475.26\angle99.92 \\
 &^2 671 - 632 \quad \text{Phase A: } 474.16\angle153.06+ 4.15\angle-35.76= 470.06\angle-26.86 \\
 & \quad \quad \quad \text{Phase B: } 200.44\angle46.63+ 15.06\angle-152.27 = 186.27\angle48.13 \\
 & \quad \quad \quad \text{Phase C: } 448.23\angle-79.33+ 28.84\angle85.86 = 420.41\angle-78.33
 \end{aligned}$$

		Current Flow in Amperes								
		Phase A			Phase B			Phase C		
Bus		IEEE	ETAP	%Diff	IEEE	ETAP	%Diff	IEEE	ETAP	% Diff
611	611	-	-	-	-	-	-	71.15	71.19	-0.06
632	RG60	558.41	558.14	-0.05	414.87	414.63	-0.06	586.60	586.31	-0.05
632	633	81.33	81.25	-0.10	61.12	61.12	0.00	62.70	62.73	-0.05
632	645	-	-	-	143.02	142.97	-0.03	65.21	65.15	-0.09
<sup>1</sup> 632	671	478.29	478.16	-0.03	215.12	214.93	-0.09	475.50	475.26	-0.09
633	632	81.33	81.25	-0.10	61.12	61.12	0.00	62.71	62.73	-0.03
633	634	81.33	81.25	-0.10	61.12	61.12	0.00	62.71	62.73	-0.03
634	633	704.83	704.19	-0.09	529.73	529.72	0.00	543.45	543.64	-0.03
645	632	-	-	-	143.02	142.97	-0.03	65.21	65.15	-0.09
645	-646	-	-	-	65.21	65.15	-0.09	65.21	65.15	-0.09
646	645	-	-	-	65.21	65.15	-0.09	65.21	65.15	-0.09
652	684	63.08	63.03	-0.08	-	-	-	-	-	-
<sup>2</sup> 671	632	470.2	470.06	-0.03	186.41	186.27	-0.08	420.64	420.41	-0.05
671	-680	-	-	-	-	-	-	-	-	-
671	-684	63.07	63.03	-0.06	-	-	-	71.15	71.19	-0.06
671	-692	229.11	229.12	0.00	69.61	69.59	-0.03	178.38	178.27	-0.06
675	692	205.33	205.37	-0.02	69.59	69.59	0.00	124.07	124.06	-0.01
680	671	-	-	-	-	-	-	-	-	-
684	671	63.07	63.03	-0.06	-	-	-	71.15	71.19	-0.06
674	611	-	-	-	-	-	-	71.15	71.19	-0.06
674	652	63.07	63.03	-0.06	-	-	-	-	-	-
692	671	229.11	229.12	0.00	69.61	69.59	-0.03	178.38	178.27	-0.06
692	675	205.33	205.37	-0.02	69.61	69.59	-0.03	124.07	124.06	-0.01

Table 3: Flow results comparison

## Reference

1. IEEE Distribution System Analysis Subcommittee for an IEEE 13-bus feeder system found on <https://cmte.ieee.org/pes-testfeeders/resources/>.
2. ETAP Unbalanced Load Flow V&V Documents, Case Number TCS-ULF-02